Standard Ob: TNB Frame, Normal Plane, and Osc	ulating Plane		
Tangent, Normal, and Binormal Vectors			
In this section we want to look at an application of	derivatives for vector-va	lued functions. We build on an application	
we saw last time: the unit tangent vector.			
unit tangent vector	, =,,	₹'(t)	
Provided 7'1t) = 0, the unit tangent vector to the	curve is given by T(t)) = r'(t) .	
example. Find the general formula for the unit tand	ent vector to the curve give	0 by =14)=2 + 3 sin(+) 3 cos(+)>	
$\frac{\vec{r}'(t)}{\vec{r}'(t)} = \frac{\vec{r}'(t)}{ \vec{r}'(t) }$	CITI VECTOV TO THE CUV VE GIVE	11 54 1 (1)= 2 5, 53111(6), 5653(6)	
7'(t) = <1, 3cos(t), -3sin(t)>			
$ \vec{r}' (t) = \sqrt{(1)^2 + (3\cos(t))^2 + (-3\sin(t))^2}$			
$= \sqrt{1 + 9 \cos^2(t) + 9 \sin^2(t)}$			
$= \int 1 + 9 (\cos^2(t) + \sin^2(t))$			
$= \sqrt{1+9} = \sqrt{10}$ 1 $3\cos(t) - 3\sin(t)$			
$T'(t) = \langle \frac{1}{\sqrt{10}}, \frac{3\cos(t)}{\sqrt{10}}, \frac{-3\sin(t)}{\sqrt{10}} \rangle$			
unit representations and the characteristics.			
Similarly, the unit normal vector to the curve is de	fined to be $\vec{\Gamma}(t) = \vec{\Gamma}'(t)$	-	
OWNTIANTY, THE WITH FLORITIAN VECTOR TO THE CANVE IS DE	TITLES TO DE TYCE? II CON		
example. Find the general formula for the unit norm	nal vector to the curve give	n by $\vec{r}'(t) = \langle t, 3\sin(t), 3\cos(t) \rangle$.	
$\vec{N}(t) = \frac{\vec{T}'(t)}{ \vec{T}'(t) }, \vec{T}(t) = \langle \frac{1}{\sqrt{10}}, \frac{3\cos(t)}{\sqrt{10}}, \frac{-3\sin(t)}{\sqrt{10}} \rangle$	Ŭ		
$\vec{\tau}'(t) = \langle 0, \frac{3}{10} \sin(t), \frac{-3}{10} \cos(t) \rangle$	Fun Facts about N(t)		
$ \vec{\tau}' _{L^{2}} _{L^{$	• N(t) 1 T(t)		
$= \int_{10}^{9} \sin^2(t) + \frac{9}{10} \cos^2(t)$	· N(t) 1 7(t)		
$= \sqrt{\frac{10}{10}} \left(\sin^2(t) + \cos^2(t) \right)$	· Nlt) should remind you of		
$\frac{1}{10} = \frac{10}{10}$ $\frac{1}{10} = \frac{10}{3\sqrt{10^{1}}} = \frac{3\cos(t)/\sqrt{10^{1}}}{3/\sqrt{10^{1}}} > \frac{3}{3/\sqrt{10^{1}}} > \frac{3}{3/\sqrt{10^{1}}$	*If		
$ N(t) = \langle 0, -\sin(t), -\cos(t) \rangle$	ex. $ \uparrow(t) = 1$ for all t then	$N(t) \perp T(t)$	
COSTUTE COSTUTE			
unit binormal vector			
Lastly, we define the unit binormal vector of a curve	e to be $\vec{B}(t) = \vec{T}(t) \times \vec{N}(t)$.		
	Big Terrible Night	mave	
example. Find the general formula for the unit binorm		$\vec{\tau}(t) = \langle t, 3 \sin(t), 3 \cos(t) \rangle$.	
$\vec{B} = \vec{T}(t) \times \vec{N}(t)$, $\vec{T}(t) = \langle \frac{1}{\sqrt{10}}, \frac{3\cos(t)}{\sqrt{10}}, \frac{-3\sin(t)}{\sqrt{10}} \rangle$, $\vec{N}(t) = \langle (\frac{1}{\sqrt{10}}, \frac{3\cos(t)}{\sqrt{10}}, \frac{-3\sin(t)}{\sqrt{10}}) \rangle$			
$\overline{B}(t) = \overline{\iota} \qquad \overline{\zeta}$ $\frac{1}{\sqrt{10'}} \qquad \frac{3\cos(t)}{\sqrt{10'}} \qquad \frac{-3\sin(t)}{\sqrt{10'}}$		Alternative Formulas:	
		$\vec{B}(t) = \frac{\vec{r}'(t) \times \vec{r}''(t)}{ \vec{r}'(t) \times \vec{r}''(t) }$ $\vec{N}(t) = \vec{B}(t) \times \vec{T}(t)$	
		N(t) = B(t) x T(t) Not Bad Today	
	nte) k		
$= \frac{-3}{100} \vec{\iota} + \frac{1}{100} \cos(t) \vec{j} + \frac{1}{100} \sin(t) \vec{k}$			
$= \langle \frac{-3}{\sqrt{10'}}, \frac{1}{\sqrt{10'}} \cos(t), \frac{1}{\sqrt{10'}} \sin(t) \rangle$			

