

The figure above describes the graph of y = f(x) and its tangent line at x = 3. Answer the problems below:

a. Estimate the average rate of change of f(x) over the interval [0,5]. average rate of change: $\frac{f(x) - f(x)}{5 - a}$ $f(5) = \frac{1}{2}$, $f(0) = \frac{3}{2}$: $\frac{f(5) - f(0)}{5 - 0} = \frac{\frac{1}{2} - \frac{3}{2}}{5 - 0} = \frac{-\frac{1}{2}}{5} = \frac{-3}{5}$ slope of gray line b. $f(3) \stackrel{?}{=} 1$ and $f'(3) \stackrel{?}{=} \frac{3}{5}$ slope of red line

c. Find the equation of the tangent line at x = 3. Give your answer in slope-intercept form.

- $\gamma 1 = -\frac{2}{3}(x-3) = \gamma 1 = -\frac{2}{3}x+2 = \gamma = -\frac{2}{3}x+3$
- **3.** The slope of the curve $y = ax^2 + bx$ at the point (2,4) is -8. Calculate the values of a and b.

4. Find the values of x for which both the graphs of the functions $f(x) = x^3 - 3x^2 + 7x + 8$ and $g(x) = \frac{1}{3}x^3 - \frac{1}{2}x^2 + 5x - 3$ have parallel tangent lines at x. Pick one such location on the graph of f(x) and find the equation of the tangent line there.

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derivative at x=2 is -8:	f'(z) = -8	•
	f'(x) = 2ax + b = -8	
	f'(z) = 2a(z)+b=-8	
	-4a+b=-8	
this is unsolvable w/o:	f(z) = 4	
	$a(z)^2 + b(z) = 4$	
	.4a+2b=4	
solve the system of equ	ations:	
(i) 4a+b=6	Chack analogs	
(ii) $40.720=7$		
Hetioa of cancenanon.	$f(x) = \frac{1}{2} + \frac{1}{2}$	•
-14a+7b=4	=-5/4) + 24	•
(0 - b) = -12		
h=17	= 4	•
substitute into eq (i):	$f'(x) = -10x \pm 12$ power rule	•
4at 17 = -8	$f'(z) = -10(z) + 12$ $\frac{d}{dz} ax^{n} = a \cdot n \times 10^{-1}$	n- 1
4a = -20	=-20+12	•
a=-5	₹-8	
<u>.</u>		
a = -5, b = 12		
equation of the tangent line there.		
parallel tangent lines m 3x ² -lex+7+0===:3x ² -==:2:2	eans $f'(x)=g'(x)$ +5-0 power rule	•
parallel tangent lines m $3x^2 - bx + 7 + 0 = \frac{1}{3} \cdot 3x^2 - \frac{1}{2} \cdot 2x^2$ $3x^2 - bx + 7 = x^2 - x + 5$	eans $f'(x)=g'(x)$ f'(x)=g'(x) $\frac{d}{dx}(ax^n)=anx^{n-1}$	•
parallel tangent lines m $3x^{2} - bx + 7 + 0 = \frac{1}{3} \cdot 3x^{2} - \frac{1}{2} \cdot 2x^{2}$ $3x^{2} - bx + 7 = x^{2} - x + 5$ $2x^{2} - 5x + 2 = 0$	eans $f'(x)=g'(x)$ +5-0 power rule $\frac{d}{dx}(ax^n)=anx^{n-1}$	•
parallel tangent lines m $3x^2 - 6x + 7 + 0 = \frac{1}{3} \cdot 3x^2 - \frac{1}{2} \cdot 2x^2$ $3x^2 - 6x + 7 = x^2 - x + 5$ $2x^2 - 5x + 2 = 0$ $2x^2 - 4x - x + 2 = 0$	eans $f'(x)=g'(x)$ f'(x)=g'(x) $\frac{d}{dx}(ax^n)=anx^{n-1}$	•
parallel tangent lines m $3x^2 - bx + 7 + 0 = \frac{1}{3} \cdot 3x^2 - \frac{1}{2} \cdot 2x^2$ $3x^2 - bx + 7 = x^2 - x + 5$ $2x^2 - 5x + 2 = 0$ $2x^2 - 4x - x + 2 = 0$ 2x(x-2) - 1(x-2) = 0 (2x-1)(x-2) = 0 2x - 1 = 0 $x - 2 = 02x = 1$ $x = 2x = \frac{1}{2}$	eans $f'(x)=g'(x)$ +5-0 power rule $dx(ax^n)=anx^{n-1}$ Note: Since $f'(x)=g'(x)$, I can use either to find the slope of the tangent line. I choose $g'(x)$ as it's simpler. But $(x,F(x)) \neq (x,g(x))$ so the tangent line of $f(x)$ at $x=\frac{1}{2}$ is parallel but not equal to the tangent line of $g(x)$ at $x=\frac{1}{2}$.	· · · · ·

5. A military craft made with a new technology that could change its velocity on demand in a moment was test driven on a long straight road. The graph of its position s(t) for eight seconds of travel is given below. Sketch in the given axes below the velocity function v(t) indicating clearly places where velocity is undefined.



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